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DFT Investigation of Structure, stability, NBO charge on Titanium-Nitrogen Nanoheterofullerenes evolved from a small nanocage

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ABSTRACT

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In this DFT (density functional theory) approach, we are performed geometric and electronic properties of Ti-N hallow cages improved from C₂₀ *i.e.*, C₂₀- $_{2n}Ti_{n}N_{n}$ (n = 1-8), at (U)B3LYP, (U)M062X, (U)B3PW91//6-311++G**, AUG-cc-pVTZ. Except for C₄Ti₈N₈, other structures are real minima and none deform as segregated open cage. Substituting causes different ΔE_{HOMO} -LUMO values (the frontier molecular orbital energy separation) and $C_{18}Ti_1N_1$ is distinguished as the suitable insulated structure, while C₁₂Ti₄N₄ is considered as the proper conductive structure. There is good reliability among polarizability, and ionization potential with substituting Ti-N units. The NICS (0) shows aromaticity decreases as n increases. Due to eight Ti-N units in the symmetrical positions of C4Ti8N8 cage, it shows dipole moment of 0.00 Debye, and the smallest charge of +0.526 on Ti. Considering the least Eads. ; -18.9 kcal/mol ; and the greatest charge of +1.269 on titaniums of $C_{18}Ti_1N_1$, it is recommended for hydrogen storage. The NBO of $C_{18}Ti_1N_1$ points out higher intramolecular charge transfer (ICT) from donor orbitals to acceptor orbitals through the appropriate overlapping between $LP(1)_N \rightarrow$ $\pi^*_{C=C}, \pi_{C=C} \rightarrow \sigma^*_{C-Ti}, \pi_{C=C} \rightarrow \sigma^*_{C-Ti}, \sigma_{C-Ti} \rightarrow \pi^*_{C=C} \text{ and } LP(1)_N \rightarrow \sigma^*_{C-Ti}$ orbitals of $C_{18}Ti_1N_1$.

1. Introduction

The C₂₀ is comprising pentagons with great curvature. Due to interesting construction of this hollow cage, it has been subject of many theoretical surveys [1-7]. Initially, interaction of C₂₀ with the lithium heteroatom does not give significant modification in the cage geometry. It is inspected to be more reactive than it's bowl and ring analogue, even though the relative energy among these isomers is influenced by sophistication of the applied theoretical methods [1-7]. It is distinguished as the most stable twenty vertex polyhedral with the minimum energy amid the mathematically probable fullerenes. From an experimental point of view, this

fullerene produced through stable C₂₀H₂₀ in gas phase [8].Furthermore, the synthesis and the doped nanosheets can be confirmed with some categorizations. Moreover, encapsulation of metal-endohedral fullerenes such as $Ti@C_{28}$, $Zr@C_{28}$, and U@C₂₈ are investigated via a bottom-up growth process [8-13]. The substituted aluminum and/or titanium heteroatoms stabilize the highly strained C_{20} , C₂₄, C₂₈ fullerenes via charge transfer (CT) from the electropositive dopant to carbon [14]. Regardless of Ti—decorated boron cages that B_{38} and B_{40} have been achieved as first experimentally the fullheterofullerene, H₂ storage of the designed transition metals at heptagon and hexagon rings of these structures have been surveyed through DFT [15].

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Experimental and theoretical inspections have revealed that Ti—clusters significantly improve H_2 storage [15]. Our enquiry further proofs theoretical insight into substituent effect of Ti—N units on C₂₀. $_{2n}Ti_nN_n$ structures, to respect which of them are suitable for H_2 storage (Figure 1).



Fig. 1. The optimized C₂₀ and its derivatives as well as their point groups, at B3LYP/AUG-cc-pVTZ.

2. Computational Methods

The optimization is done for closed-shell multiplicity (n = 0, 2, 4, 6, 8) at the restricted spin-symmetry methods and for opened-shell multiplicity (n = 1, 3, 5, 7) at the unrestricted spin-symmetry methods using the GAMESS [16-18]. Harmonic frequencies are obtained to realize nature

and ZPVE value [18]. The NBO [19], aromaticity [20], MEP as well as reactivity [21] calculations are individually achieved, at three methods. The reactivity is accomplished via $N = E_{\text{HOMO(Nu)}} - E_{\text{HOMO(tetracyanoethylene)}}$, $\omega = \mu^2 / 2\eta$, $\mu = (E_{\text{HOMO}} + E_{\text{LUMO}}) / 2$, $\eta = (E_{\text{LUMO}} - E_{\text{HOMO}}) / 2$, $\chi = -\mu$, $S = 1 / 2\eta$, and $\Delta N_{\text{max}} = -\mu / \eta$.

3. Results and Discussion

In the succeeding parts we will discuss substituted heteroatom effects by increasing the Ti—N units, however there are many other likely isomers but we are investigated eight of them.

3.1.Structural investigation

The structures of studied molecules are explained in terms of bond distances close to the substituting elements. The C—C bond distances of C_{20} are around 1.44 - 1.54 Å (Tables 1 and 2) which insert amid the values of H₂C=CH₂ and H₃C—CH₃ (1.35 and 1.54 Å, respectively).

Table 1. The bond lengths per Å, at B3LYP/AUG-cc-
pVTZ.

Species	C=C	Ti–C	N-C
C ₂₀	1.444-1.537	-	-
C18Ti1N1	1.398-1.538	1.444	1.443
C16Ti2N2	1.410-1.523	2.006- 2.021	1.408- 1.432
C14Ti3N3	1.397-1.501	1.877- 2.074	1.424- 1.491
C12Ti4N4	1.402-1.493	1.079- 2.080	1.395- 1.448
C10Ti5N5	1.402-1.523	1.587- 1.609	1.587- 1.609
C8Ti6N6	1.336-1.482	1.943- 2.165	1.355- 1.488
C6Ti7N7	1.408-1.414	2.117- 2.162	1.376- 1.419
C4Ti8N8	1.449	-	1.375

Table 2. The bond lengths per Å, at B3LYP/AUG-cc-pVTZ.

Species	Ti–N	Ti–Ti
C ₂₀	-	
$C_{18}Ti_1N_1$	1.442	-
C16Ti2N2	2.006-2.027	2.380
C14Ti3N3	1.953-1.984	-
C ₁₂ Ti ₄ N ₄	2.041-2.065	2.305
C10Ti5N5	1.674-1.697	-
C ₈ Ti ₆ N ₆	1.882-2.031	2.502-2.775
C6Ti7N7	1.872-2.078	2.701-2.798
C4Ti8N8	1.873-2.028	2.360

The considered Ti—C, and N—C bond lengths are expanded to approximately 1.77 - 2.61 Å which are followed with sum of covalent radii of the scrutinized atoms; C = 0.70 Å, Ti = 1.40 Å and N = 0.65 Å. Shrinking 0.11 Å in C=C bond length of heterofullerenes *vs.* C₂₀ is attributed to dopants. The bond angles of C–Ĉ–C (99.59° – 118.82°), C–Ti–C (37.03° – 91.73°), and C–N–C (98.74° – 113.96°) are changed *vs.* C–Ĉ–C (103.99° to 111.31°) of pure C₂₀ (Table 3).

 Table 3. The bond angles (in degree), at B3LYP/AUG-ccpVTZ.

Species	C-C-C	C-Ti-C	C-N-C
C20	103.99- 111.31	-	-
C18Ti1N1	103.46- 117.93	85.79	101.64
C ₁₆ Ti ₂ N ₂	99.59- 118.82	-	99.81- 99.94
C14Ti3N3	103.75- 132.89	83.81- 117.40	89.89- 105.85
C12Ti4N4	99.78- 114.38	-	98.74- 99.63
C10Ti5N5	107.33- 108.77	38.92- 39.89	-
C8Ti6N6	-	37.03- 74.44	104.66- 113.96
C6Ti7N7	-	91.73	108.16
C4Ti8N8		-	-

These variations create pyramidalization on dopant sites; $\theta_C = 360 - [(C-C-C)_1 + (C-C-C)_2 + (C-C-C)_3]$, $\theta_{Ti} = 360 - [(C-Ti-C)_1 + (C-Ti-N)_2 + (N-Ti-C)_3]$ and $\theta_N = 360 - [(C-N-C)_1 + (C-N-Ti)_2 + (Ti-N-C)_3$ (Table 4) [22-25].

Table 4. The pyramidalization angles of θ_{Ti} , θ_N (in degree), at B3LYP/AUG-cc-pVTZ. The pyramidalization angle of C₂₀ is $31.623 - 42.254^{\circ}$.

Species	θτι	θΝ
C20	31.62-42.25	-
$C_{18}Ti_1N_1$	100.95	40.84
C ₁₆ Ti ₂ N ₂	64.22	35.5
C ₁₄ Ti ₃ N ₃	26.25-98.52	34.28-101.16
C12Ti4N4	72.33-123.25	32.06-49.44
C10Ti5N5	-	-
C8Ti6N6	-	35.32-115.38
C ₆ Ti ₇ N ₇	23.39-71.26	40.86-92.14
C4Ti8N8	76.85	40.23

Here, the substituting dopants of $C_{20-2n}Ti_nN_n$ species displays more pyramidalization vs. C_{20} , owing to their more tendency to accept sp^3 hybridization than sp^2 . The smallest vibrational frequency (v_{min}) analysis displays one negative frequency only for $C_4Ti_8N_8$ as transition state and positive frequencies for others as real minima (Table 5 and Figure 2).

Table 5. The total energy, smallest vibrational frequency,polarizability, and polarity.

	$\frac{E_{\text{tot}}^{a, (b), c, [d]}}{E}$	Umin ^e /	h	h	
Species	a.u.	cm ⁻¹	<α>»	μυ	
Cas	-761.60234	82.23	187.27	0.00	
C20	(-761.18425)	62.25	107.27	0.00	
	-761.18350				
	[-761.67038]				
	-1589.47147				
CasTiaNa	(-1589.11869)	127.09	184.04	5.96	
Claring	-1589.35354				
	[-1589.77347]				
CirTiaNa	-2417.44789	104 94	243 27	5.95	
C10112112	(-2417.12013)	104.74	2-3.27	5.75	
	-2417.33158				
	[-2417.83232]				
CuTiaNa	-3245.52935	137.84	250.89	5 64	
C14113133	(-3245.15983)	157.04	230.07	5.04	
	-3245.35522				
	[-3245.95661]				
C12Ti4N4	-4073.41358				
	(-4073.102759)	75.13	483.89	0.54	
	-4073.29079				
	[-4073.953506]				
CiaTisNe	-4901.89785	158 28	298 21	4 37	
C10115145	(-4901.57717)	150.20	270.21	т.57	
	-4901.77369				
	[-4902.461001]				
CoTicNe	-5729.82262	109 37	304 89	3 1 2	
	(-5729.56165)	109.57	504.07	5.12	
	-5729.68969				
	[-5730.50202]				
CeTi7N7	-6557.772910	91 56	398 25	1 54	
C61171N7	(-6557.71081)	71.50	570.25	1.51	
	-6557.84980				
	[-6558.02788]				
C4TieNe	-7386.224877	-269.67	633 14	0.00	
V4 I 181 18	(-7385.58105)	207.07	055.14	0.00	
	-7385.68065				
	[-7385.81647]				
A+ aDC	VD/c 211 + C*	≥ b \// (16 DV/6 21	$1 \cdot \cdot C * *$	

At ^aB3LYP/6-311++G**, ^bM06-2X/6-311++G**, ^cB3PW91/6-311++G**, ^dB3LYP/AUG-cc-pVTZ, and ^eB3LYP/6-311+G*.



C₄Ti₈N₈

Fig. 2. The selected IR spectrum of C_{20} , $C_{18}Ti_1N_1$ and $C_4Ti_8N_8$, at B3LYP/6-311+G*.

Here, the E_{tot} is increased as n is increased and $C_{18}Ti_1N_1$, $C_{16}Ti_2N_2$, $C_{10}Ti_5N_5$, and $C_8Ti_6N_6$ structures compare to C_{20} fulfill "stability conditions" showing the v_{min} values of 127.09, 104.94, 158.28, and 109.37

cm⁻¹, which are high *vs.* 82.2 cm⁻¹ [26]. Interestingly, there is good consistency between $\langle \alpha \rangle$ and the order of n. The $\langle \alpha \rangle$ is improved from 187.27 *a.u.* for C₂₀ to 633.14 *a.u.* for C₄Ti₈N₈. It seems that the substituted Ti, N heteroatoms in C_{20-2n}Ti_nN_n heterofullerens lead to increasing $\langle \alpha \rangle$ and C₄Ti₈N₈ has more tendency to interaction with the neighboring polar molecule. The substituted doping C₂₀ to C₁₈Ti₁N₁, C₁₆Ti₂N₂, C₁₀Ti₅N₅, C₈Ti₆N₆, and C₆Ti₇N₇ is caused considerably μ of 5.96, 5.96, 4.37, 3.12, and 1.54 Debye, respectively (Table 5).

3.2. $\Delta E_{HOMO-LUMO}$, IE or IP, and NICS

One Ti—N bond of $C_{18}Ti_1N_1$ is increased the $\Delta E_{\text{HOMO-LUMO}}$ (1.79, 2.06, 1.80 eV) leading to enhanced stability against electronic excitations (Table 6).

Table 6. The FMO (in *a.u.*), along with band gap (in eV).

Species	$E_{\text{HOMO}}^{a, (b),}$	<i>E</i> _{LUMO} ^{a, (b),} [c]	$\Delta E_{\text{HOMO-LUMO}^{a}}$
	-0.20134	-0.13054	1.93
C20	(-0.21055)	(-0.12567)	(2.31)
	[-0.20455]	[-0.13351]	[1.93]
	-0 19002	-0 15070	1 79
CusTinNa	(-0.19002)	(-0.13070)	(2.06)
	[-0.19241]	[-0.12624]	[1.80]
	-0.17362	-0.11566	1.58
C ₁₆ Ti ₂ N ₂	(-0.18059)	(-0.11286)	(1.84)
	[-0.17470]	[-0.11676]	[1.58]
	0.10101	0 100 15	1.42
~	-0.19181	-0.13945	1.42
C ₁₄ Ti ₃ N ₃	(-0.14289)	(-0.07834)	(1.76)
	[-0.13560]	[-0.08806]	[1.29]
	-0 13989	-0 10388	0.98
CuTiANA	(-0.13985)	(-0.10964)	(0.82)
012114114	[-0.13950]	[-0.10395]	[0.97]
	-0.17146	-0.10626	1.77
C ₁₀ Ti ₅ N ₅	(-0.17086)	(-0.10488)	(1.80)
	[-0.17365]	[-0.10643]	[1.83]
	0 1 42 50	0.00207	1.62
	-0.14359	-0.08387	1.63
C8T16N6	(-0.14230)	(-0.08321)	(1.61)
	[-0.14680]	[-0.07/01]	[1.20]
	-0.1/000	-0.09408	1 27
C _c Ti-N-	(_0 1/088)	(_0 00677)	(1.2)
C611/14/	[-0.14581]	[-0.10790]	[1.03]
	-0.13346	-0.08443	1.33
C4Ti8N8	(-0.13258)	(-0.08651)	(1.25)
	[-0.12279]	[-0.08700]	[0.97]

At "B3LYP/AUG-cc-pVTZ, "M06-2X/6-311++G**, and "B3PW91/6-311+G*.

Four Ti-N bonds of C12Ti4N4 are decreased the $\Delta E_{\text{HOMO-LUMO}}$ of 0.98 eV at B3LYP/AUG-cc-pVTZ, 0.82 eV at M06-2X/6-311++G**, 0.97 eV at B3PW91/6-311+G* and leading to the enhanced conductivity of C12Ti4N4. Hence, C18Ti1N1 is distinguished as the most kinethic stable derivative, whereas C₁₂Ti₄N₄ with four separated Ti-N units via four C=C bonds is classified as the least kinethic stable one. Also, we are evaluated the ionization energy or ionization potential (IE or IP) (Table 7). Now, to probe proper connection, we compare $\Delta E_{\text{HOMO-LUMO}}$, IE or IP, and aromaticity based on NICS (0) of C_{20} and heterofullerenes with n. The $\Delta E_{\text{HOMO-LUMO}}$ value of heterofullerenes is lower than that of C₂₀, and there is no uniformity amid band gap and n (Figure 3).

Table 7. The ionization potential, and NICS (0), at B3LYP/AUGcc-pVTZ.

Species	IE (IP)	NICS (0)	NICS (0) _{ZZ}
C20	167.75	-23.81	3.69
C ₁₈ Ti ₁ N ₁	162.07	-42.05	-60.98
C16Ti2N2	156.31	-37.82	-52.03
C ₁₄ Ti ₃ N ₃	150.81	-19.50	-35.12
C ₁₂ Ti ₄ N ₄	145.09	-15.72	-55.32
C10Ti5N5	139.42	-13.51	-40.83
C8Ti6N6	133.69	-19.94	-30.89
C6Ti7N7	127.74	-13.42	-16.05
C4Ti8N8	121.87	-16.10	-25.16



Fig. 3. The relationship between band gap and n, at B3LYP/AUG-cc-pVTZ.

The formations of these nanocages are quite complicated due to the possibility of high-spin states. Such possibilities arise due to insertion of Ti $({}^{3}F_{2})$ and N $({}^{4}S_{3/2})$ of atoms in C₂₀. The band gap values reveal different electronic charge-transfer possibilities within the considered molecules, while Ti—N units are increased in the fullerenes. The IE or IP value of C₂₀.

 $_{2n}$ Ti_nN_n heterofullerens is decreased with increasing n (Figure 4).



Fig. 4. The relationship between ionization potential and n. We are obtained isotropic parameter of -23.8 ppm for C_{20} , which indicates strong aromaticity of it *vs*. benzene (-8.5 ppm) (Table 7). The $C_{20-2n}Ti_nN_n$ heterofullerenes show different NICS (0) from -42.05 to -13.42 ppm and they are aromatic. Furthermore, the studied heterofullerenes exhibit NICS (0)zz from -60.98 ppm for $C_{18}Ti_1N_1$ to -16.05 ppm for $C_6Ti_7N_7$ which imply strong ring current *vs*. benzene (-10.17 ppm). With increasing n, the delocalized π -electrons are shifted from more Ti heteroatoms to neighboring atoms (Figure 5).



Fig. 5. The relationship between aromaticity and n.

Even though the electronegativity difference is significant, π -delocalization effect on the ring perimeter is strengthened in $C_{18}Ti_1N_1$ derivative, while such ring current is weakened in other

derivatives. Thus, the isotropic polarizability $\langle \alpha \rangle$ is modified depending on n and dopant topology (Figure 6).



Fig. 6. The relationship between polarizability and n. 3.3. NBO charge, MEP, and hydrogen adsorption Obviously, the NBO charges of derivatives are not equivalent; so that the negative charge on N sites is changed from -0.973 to -0.589e and the positive charge on Ti sites is improved from +0.527 for C₄Ti₈N₈ to +1.269 for C₁₈Ti₁N₁ (Figure 7).





 $C_{18}Ti_1N_1$



 $C_{14}Ti_3N_3\\$



 $C_{16}Ti_2N_2$



 $C_{12}Ti_4N_4$



 $C_6Ti_7N_7$ $C_4Ti_8N_8$ Fig. 7. The NBO charge on atoms of C20 and heterofullerenes, at B3PW91/6-311++G**.

Based on Froudakis's findings, $C_{18}Ti_1N_1$ is as the suggested species for H₂ storage [23]. The MEP is displayed though red—blue colors on Ti—N surfaces indicating their dispersed charges, correspondingly (Figure 8).



 $C_{10}Ti_5N_5$ $C_6Ti_7N_7$ Fig. 8. Three-dimensional MEP of the selected derivatives, at B3PW91/6-311++G**.

We are probed H₂ adsorption on one to eight Ti and N-modified heterofullerenes using DFT simulations to introduce suitable systems for the storage of H₂ molecules. We have not used number of the Ti and N heteroatoms more than eight in C₂₀; because the optimized heterofullerenes with the molecular formula of C_{20-2n}Ti_nN_n (n > 8) are collapsed to the segregated open cage structures. The mixed transition metal

(titanium) and the main element of the periodic table (nitrogen with more electronegative than boron element) have been chosen, because the results of previous studies displayed that the interaction between H₂ molecules and Ti-decorated B₃₈ and B₄₀ fullerenes as the modified adsorbent materials are stronger than those of the other transition metals modified systems [13]. The hydrogen adsorption is designed by reaction of $C_{20-2n}Ti_nN_n + 2H_2 \rightarrow C_{20-2n}Ti_nN_n....(H_2)_2$. The overall trend of $|E_{ads.}|$ (in kcal/mol) for two H₂ -27.54 > $C_{12}Ti_4N_4$ | -25.72 | > $C_{14}Ti_3N_3$ $|-23.22| > C_{16}Ti_2N_2| -21.08| > C_{18}Ti_1N_1| -18.9|$ vs. C_{20} (+81.1). Next, the theoretical work needs to be supported more in its theoretical form. Thus, we are added n H₂ to the titanium and nitrogen heteroatoms. Compared to 1Ti/B₃₈/(H₂)₁ complex with capacity of 2.56 wt% and $|E_{ads.}|$ of 0.22 eV/H₂; here C_{20-2n}Ti_nN_n systems show higher capacity. Each Ti-N unit can bind up to $2H_2$ with $|E_{ads.}|$ of 0.07 eV/H₂. For example, additional 10H₂ molecules can be absorbed to 10H₂/C₁₀Ti₅N₅ complex with capacity of 4.48 wt% and $|E_{ads.}|$ of 0.37 eV/H₂. Hence, the net NBO positive charge of the Ti heteroatom is decreased from +1.269 to +0.6680 also, the net NBO negative charge of the nitrogen heteroatom is decreased from |-0.701e| to |-0.232e|.

3.4.Reactivity

Substituting of Ti—N units is led to various modifications of N, ω , μ , η , χ , S, and ΔN_{max} (Table 8).

Table 8. The reactivity parameters (in eV), at M06-2X/6-311++G**.

Species	N	ω	μ	η	χ	S	$\Delta N_{\rm ma}$
C20	3.73	4.53	-4.57	2.31	4.57	0.2	1.98
C18Ti1 N1	4.15	4.46	-4.28	2.06	4.28	0.2 4	2.08
C ₁₆ Ti ₂ N ₂	4.55	4.32	-3.99	1.84	3.99	0.2 7	2.17
C14Ti3 N3	5.57	2.58	-3.01	1.76	3.01	0.2 8	1.71
C12Ti4 N4	5.65	7.01	-3.39	0.82	3.39	0.6 1	4.13
C10Ti5 N5	4.81	3.92	-3.75	1.80	3.75	0.2 8	2.09
C ₈ Ti ₆ N	5.59	2.93	-3.07	1.61	3.07	0.3	1.91
C6Ti7N	5.63	4.35	-3.23	1.20	3.23	$0.4 \\ 2$	2.69
C4Ti8N	5.85	3.54	-2.98	1.25	2.98	0.4	2.38

Regardless $C_{10}Ti_5N_5$, *N* is increased nearly with increasing n (from 3.73 eV for C_{20} vs. 4.15 eV for $C_{18}Ti_1N_1$ to 5.85 eV for $C_4Ti_8N_8$). Moreover, three, and four substituted Ti—N unit structure is the least, and most electrophile species (2.58, and 7.01 eV for C₁₄Ti₃N₃, and C₁₂Ti₄N₄, respectively, *vs.* 4.53 eV for C₂₀). C₁₈Ti₁N₁ contains the minimum *N*, *S*, and the maximum χ , η , and absolute μ among eight analogues. In contrast, C₁₂Ti₄N₄ includes the least η and the most ω , *S*, and ΔN_{max} . Hence, C₁₈Ti₁N₁, and C₁₂Ti₄N₄ are the least, and the most chemically reactive species, singly. The lowest and the highest positive ΔN_{max} is demonstrated for C₁₄Ti₃N₃ and C₁₂Ti₄N₄ as the weakest and the strongest electron acceptor from other donors.

3.5. NBO analysis

Here, we are focused on NBO analysis of $Ti_1N_1C_{18}$ species (Tables 9 and 10).

Table 9. The occupancy of the intramolecular bonds in $Ti_1N_1C_{18}$, at M06-2X/6-311++G**.



Bond	Occup.	ED _A (%)	ED _B (%)
π C3 = C10	0.74318	43.41	56.59
σ C7 — Ti20	0.86892	47.47	52.53
σ C8 – C9	0.98876	49.88	50.12
σ C15 — N19	0.98465	40.01	59.99
σ C18 — N19	0.98498	40.16	59.84
LP(1) _{N19}	0.72270		
LP(1)Ti20	0.73941		

Table	10.	The	NBO,	and	hybridizations	of	the
intramo	lecula	r bond	ls in Ti 1N	N_1C_{18} ,	at M06-2X/6-31	1++C	j**.



Bond	NBO	s (%)	p (%)	d (%)
$\pi_{C3 = C10}$	$\begin{array}{c} 0.6589^* sp^{99.99} d^{2.69} \\ + 0.7523^* sp^{99.99} d^{1.30} \end{array}$	0.07, 0.08	99.75, 99.81	0.18, 0.11
$\sigma_{\rm C7-Ti20}$	$\begin{array}{l} 0.6890^*sp^{47.82}d^{0.01} \\ +0.7247^*sp^{0.10}d^{56.24} \end{array}$	2.05, 1.74	97.93, 0.17	0.03, 98.07
σ C8 – C9	$\begin{array}{l} 0.7062^*sp^{2.00}d^{0.00} \\ +0.7080^*sp^{1.99}d^{0.00} \end{array}$	33.28, 33.37	66.64, 66.55	0.08, 0.08
σ _{C15} – N19	$\begin{array}{l} 0.6325^*sp^{2.54}d^{0.00} \\ +0.7745^*sp^{2.10}d^{0.00} \end{array}$	28.21, 32.19	71.67, 67.74	0.13, 0.07
σ _{C18} – _{N19}	$\begin{array}{l} 0.6337^* \; sp^{2.53} d^{0.00} \\ + 0.7736^* sp^{2.14} d^{0.00} \end{array}$	28.29, 31.87	71.59, 68.07	0.13, 0.06
LP(1) _{N19}	sp ^{99.99} d ^{0.97}	0.05	99.89	0.05
LP(1) _{Ti20}	sp ^{0.08} d ^{99.99}	0.73	0.06	99.21

The first two columns show the type of orbital and occupancy between 0.98876 electrons for σ_{C8-C9} bonding orbital with sp^2 hybrid vs. 0.72270, and 0.73941 electrons for LP(1)_{N19}, LP(1)_{Ti20} lone pairs sp^{0.08}d^{99.99} $sp^{99.99}d^{0.97}$, with and hybrids, correspondingly. The sp^2 hybrid on C₈, and C₉ atoms of C₈—C₉ sigma bond has 33.28, and 33.37% s, 66.64, and 66.55% p-character, respectively. Also, the $sp^{99.99}d^{0.97}$ hybrid on lone pair of N₁₉ has 0.05% s, 99.89% p, and 0.05% d-character. While, the $sp^{0.08}d^{99.99}$ hybrid on lone pair of Ti₂₀ has 0.73% s, 0.06% p, and 99.21% d-character. The occupancy of $\sigma_{C7-Ti20},~\sigma_{C15-N19},$ and $\sigma_{C18-N19}$ is 0.86892, 0.98465, electrons, 0.98498 and with $0.6890*sp^{47.82}+0.7247*sp^{0.10}d^{56.24},$ $0.6325*sp^{2.54}+0.7745*sp^{2.10}$ and

 $0.6337*sp^{2.53}+0.7736*sp^{2.14}$ hybrid, respectively. Evidently, hetero bonding orbitals of $\sigma_{C7-Ti20}$, $\sigma_{C15-Ti20}$ _{N19}, and $\sigma_{C18-N19}$ have 47.47% C₇, 40.01% C₁₅, 40.16% $C_{18},\ 52.53\%$ $Ti_{20},\ 59.99\%$ $N_{19},\ and\ 59.84\%$ N₁₉ characters in their corresponding hybrids, respectively. Therefore, titanium and nitrogen heteroatoms have the more percentage of NBOs and gives the more polarization coefficients (0.7247, 0.7745, and 0.7736) than the homo bonding bonds (C—C and/or C=C) because typical titanium has low ability to form hybrid orbitals and prefers $[Ar](4s^2)(3d^2)$ valence electronic configuration which leads to the divalent doublet ground state, and nitrogen has the higher electronegativity than carbon atom. The more important $E^{(2)}$ of Ti₁N₁C₁₈ is related to LP(1)_{N19} $\rightarrow \pi^*_{C17=C18}, \pi_{C8=C9} \rightarrow \sigma^*_{C7-Ti20}, \pi_{C6=C15} \rightarrow \sigma^*_{C7-Ti20},$ $\sigma_{C7-Ti20} \rightarrow \pi^*_{C8=C9}$ and LP(1)_{N19} $\rightarrow \sigma^*_{C7-Ti20}$ orbital's and their corresponding energy is 10.03, 7.07, 6.58, 5.83, and 3.42 kcal/mol, correspondingly (Table 11).

Table 11. The $E^{(2)}$ of the intramolecular bonds in $Ti_1N_1C_{18}$, at M06-2X/6-311++G**.

C145C15C.C6	
C13 C4 N19 C2 C7	
C12 ^{C18} C3 Ti203	
C1C17_:C169	

Donor NBO (i)	Acceptor NBO (j)	$E^{(2)}$ (kcal/mol)
$\pi_{C8} = C9$	σ* C7 — Ti20	7.07
π C6 = C15	LP*(2) _{Ti20}	0.30
$\pi_{C6} = C15$	σ*c7 — Ti20	6.58
σ C7 — Ti20	π^* C8 = C9	5.83
σ C7 — Ti20	σ *C9 – C16	0.26
LP(1) _{N19}	σ *C7 — Ti20	3.42
LP(1) _{N19}	π^* C17 = C18	10.03

These interactions is resulted from the electron donating of the bonding orbitals to the electron acceptoring anti-bonding orbitals, indicating higher CT is happened in these orbitals, compared to lower CT from $\pi_{C6=C15}$ to LP*(2)_{Ti20}, and from $\sigma_{C7-Ti20}$ to σ^*_{C9-C16} with $E^{(2)}$ of 0.30, and 0.26 kcal/mol, respectively.

4. Conclusions

Substituent effects of Ti-N units on geometry, $\Delta E_{\text{HOMO-LUMO}}$, ionization potential, aromaticity, NBO charge of C_{20} derivatives are accessed, at DFT. The vibrational frequency calculations imply exclusive of C₄Ti₈N₈ species, reminders are real minima and none of analogous collapse to open deformed cage. The $\Delta E_{\text{HOMO-LUMO}}$ of 1.79, 2.06, and 1.80 eV proposes the $C_{18}Ti_1N_1$ as the most kinetic stable and the weakest conductive structure. Also, the $\Delta E_{\text{HOMO-LUMO}}$ of 0.98, 0.82, and 0.97 eV suggests the $C_{12}Ti_4N_4$ with four separated Ti-N units via 4 C=C bonds as the least kinetic stable and the strongest conductive system. The calculated IE (IP) of 162.07 kcal/mol, NICS (0) of -42.05 ppm and NICS (0)_{ZZ} of -60.98 ppm display C₁₈Ti₁N₁ that in which one Ti—N unit is replaced to two neighboring carbon atoms, as the most thermodynamic stable and the most aromatic nanocage. The most and the least charge on Ti of $C_{18}Ti_1N_1$ (+1.269) and $C_4Ti_8N_8$ (+0.527), also the least and the most $|E_{ads.}|$ of -18.9 and -33.20 kcal/mol, leads to increasing and decreasing capacity of $C_{18}Ti_1N_1$ and $C_4Ti_8N_8$ for hydrogen storage, respectively. Furthermore, in going from $C_{18}Ti_1N_1$ to $C_4Ti_8N_8$, as n increases both nucleophilicity index (N), and chemical potential (μ) increase with C₁₈Ti₁N₁ and C₄Ti₈N₈ turning out as the least and most nucleophilic species, respectively, while electronegativity (χ) decreases. The MEP maps qualitatively verify the nucleophilicity strength. The NBO analysis of $C_{18}Ti_1N_1$ points out higher ICT including $LP(1)_N \rightarrow$ $\pi^*_{C=C},\,\pi_{C=C}\rightarrow\sigma^*_{C-Ti},\,\pi_{C=C}\rightarrow\sigma^*_{C-Ti},\,\sigma_{C-Ti}\rightarrow\pi^*_{C=C}$ and LP(1)_N $\rightarrow \sigma^*_{C-Ti}$ orbitals.

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